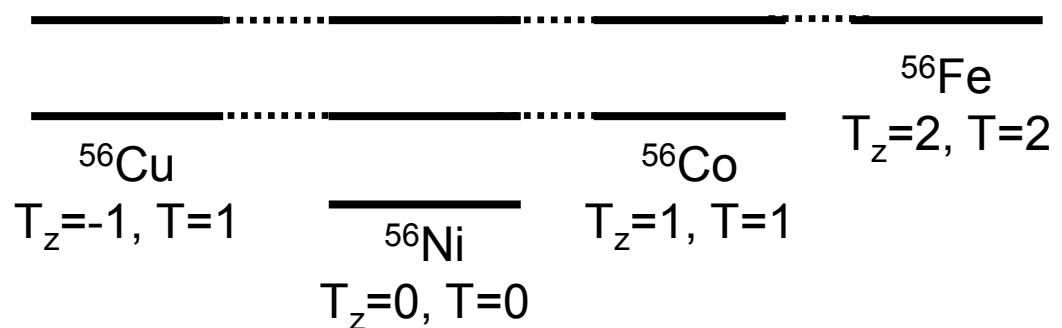


And now for something completely different

# Isospin

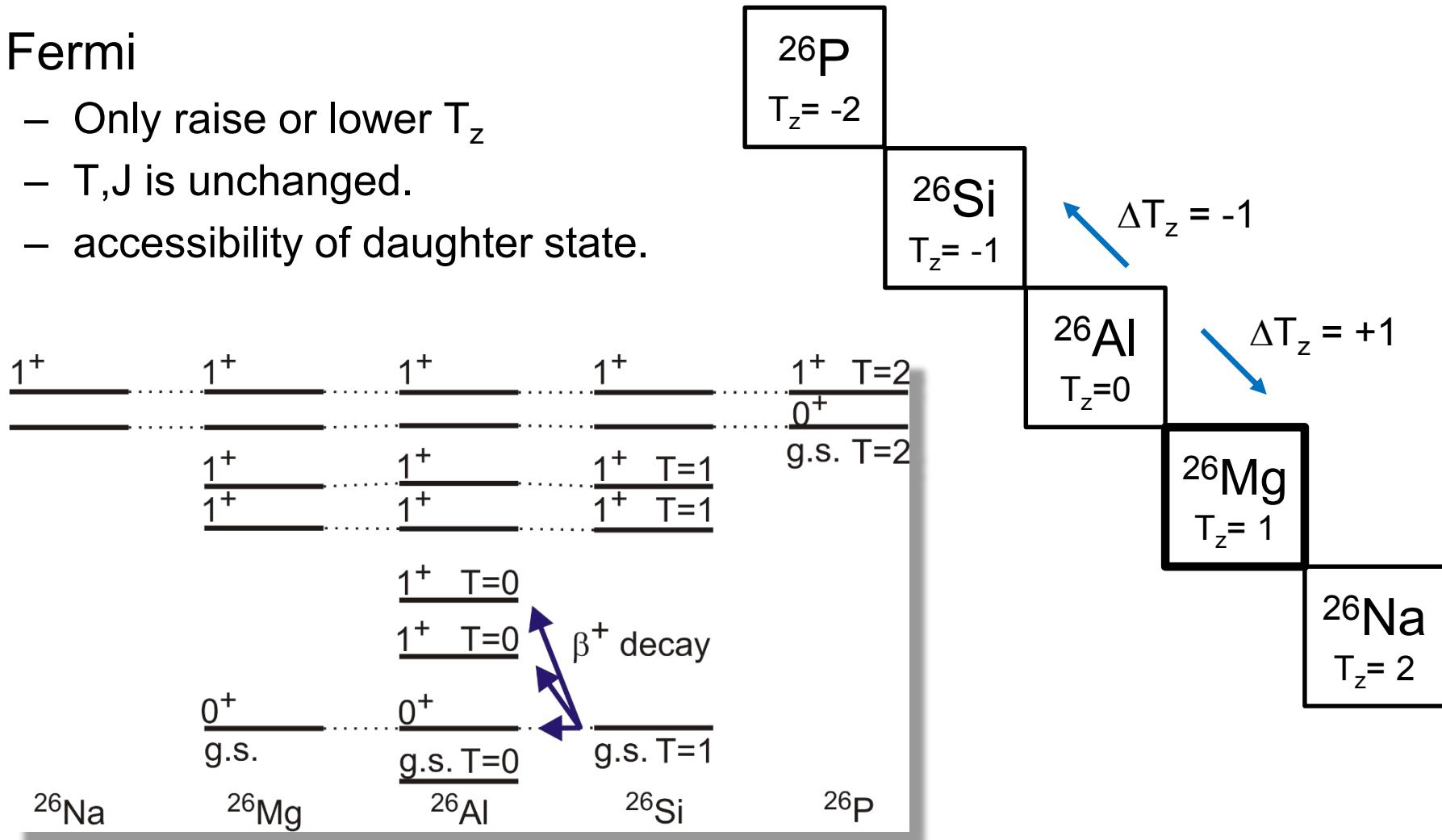
- Isospin formalism
  - assume nuclear force is charge independent.
- Introduce isospin,  $T$ 
  - Proton,  $T = \frac{1}{2}$ ,  $T_z = -\frac{1}{2}$
  - Neutron,  $T = \frac{1}{2}$ ,  $T_z = \frac{1}{2}$
  - $T_z = (N-Z)/2$
- General rule:
  - $T$  has lowest possible value for given  $T_z$ .

$^{56}\text{Cu}$	$^{57}\text{Cu}$	$^{58}\text{Cu}$	$^{59}\text{Cu}$
$^{55}\text{Ni}$	$^{56}\text{Ni}$	$^{57}\text{Ni}$	$^{58}\text{Ni}$
$^{54}\text{Co}$	$^{55}\text{Co}$	$^{56}\text{Co}$	$^{57}\text{Co}$
$^{53}\text{Fe}$	$^{54}\text{Fe}$	$^{55}\text{Fe}$	$^{56}\text{Fe}$



# Fermi Matrix Elements

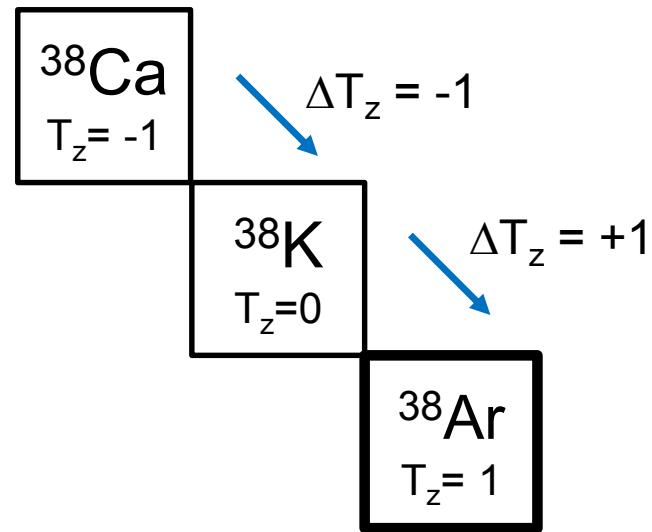
- Fermi
  - Only raise or lower  $T_z$
  - $T, J$  is unchanged.
  - accessibility of daughter state.



Courtesy R. Zegers

# Super allowed Fermi transitions

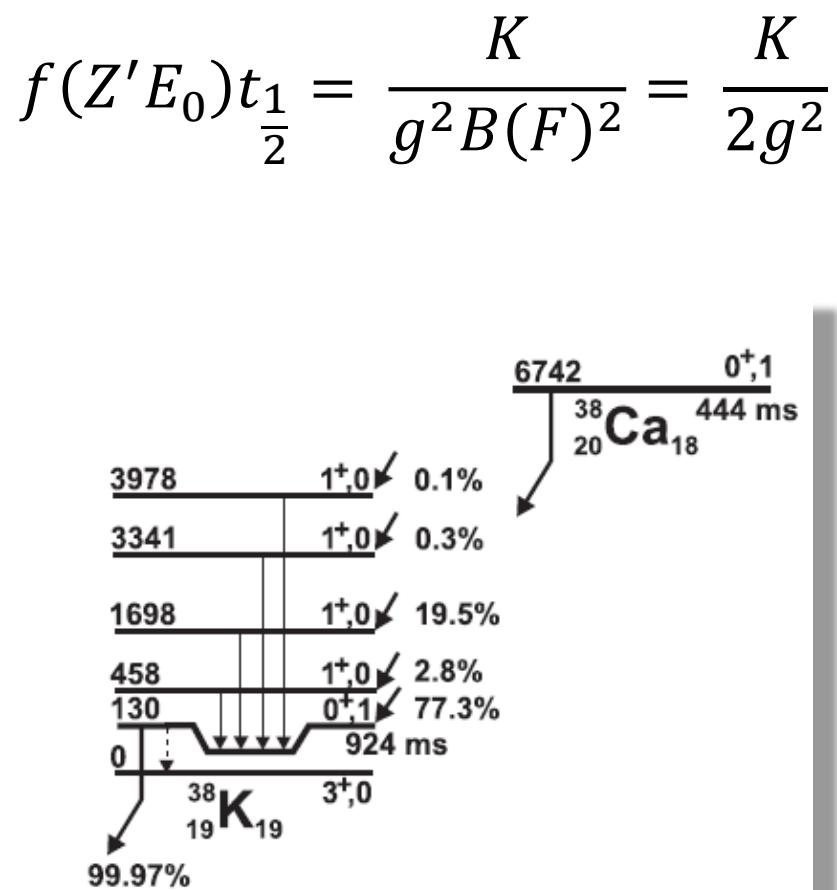
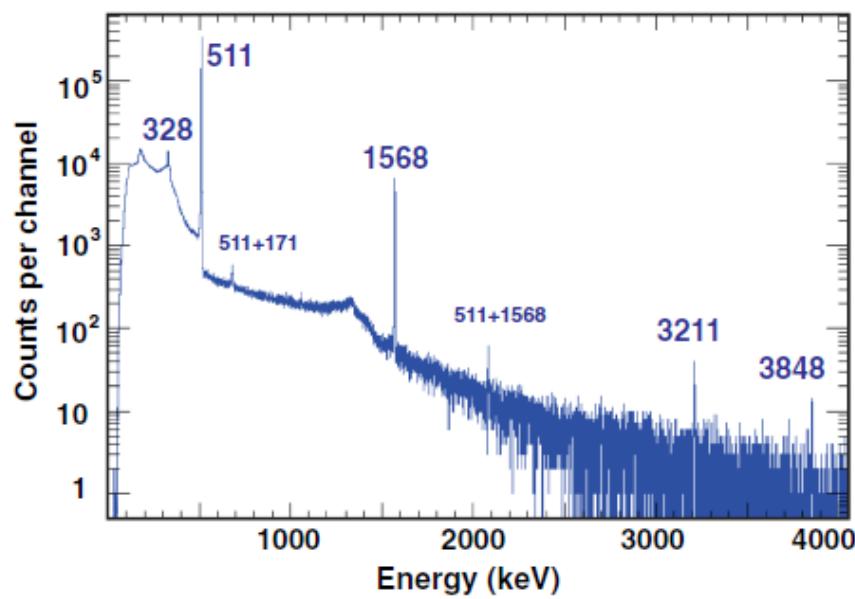
- Standard model test
- Super allowed Fermi Transitions
  - $0^+ \rightarrow 0^+$  transitions
  - Same T
  - Gamow-Teller can't contribute
- Simple matrix element
- Constant log $f\tau$



$$f(Z'E_0)t_{\frac{1}{2}} = \frac{K}{g^2 B(F)^2} = \frac{K}{2g^2}$$

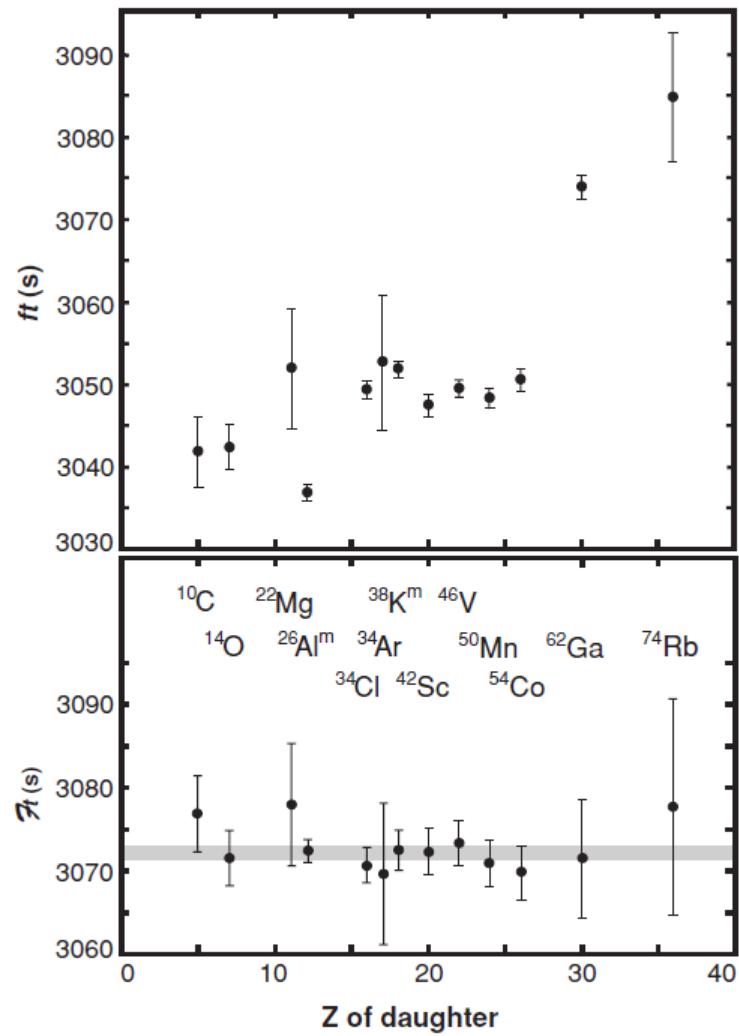
# Super allowed Fermi transitions: A = 38

- Experimental Constraints
  - $T_{1/2}$ , branching ratios to 0.05%
  - Masses to 100's eV
  - Understanding of corrections



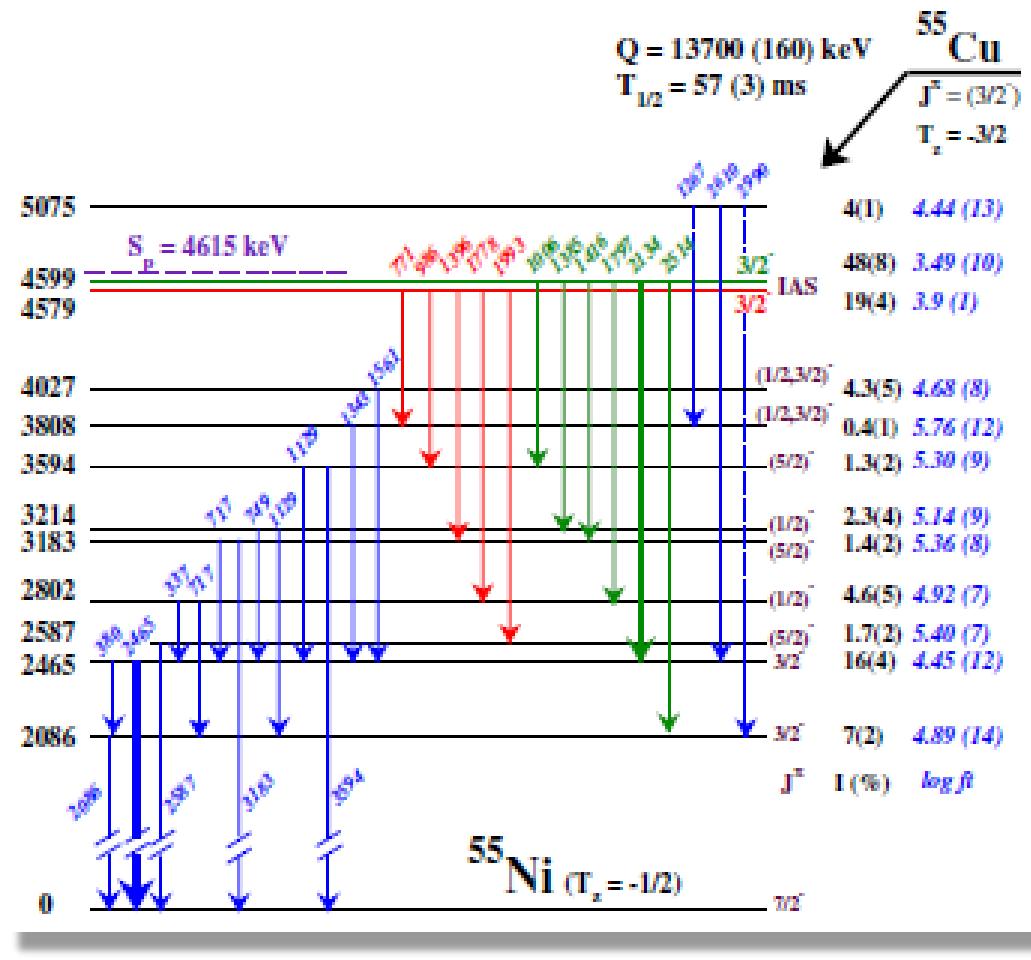
# Super allowed Fermi transitions: All data

- Uncorrected ft values
  - Large spread due to corrections
- Corrected ft values
  - Isospin-symmetry breaking
  - Radiative corrections
- Current value
  - 3072 s



# Isospin mixing

- Isospin not perfect.
- States with same  $J^\pi$  and different isospin can mix



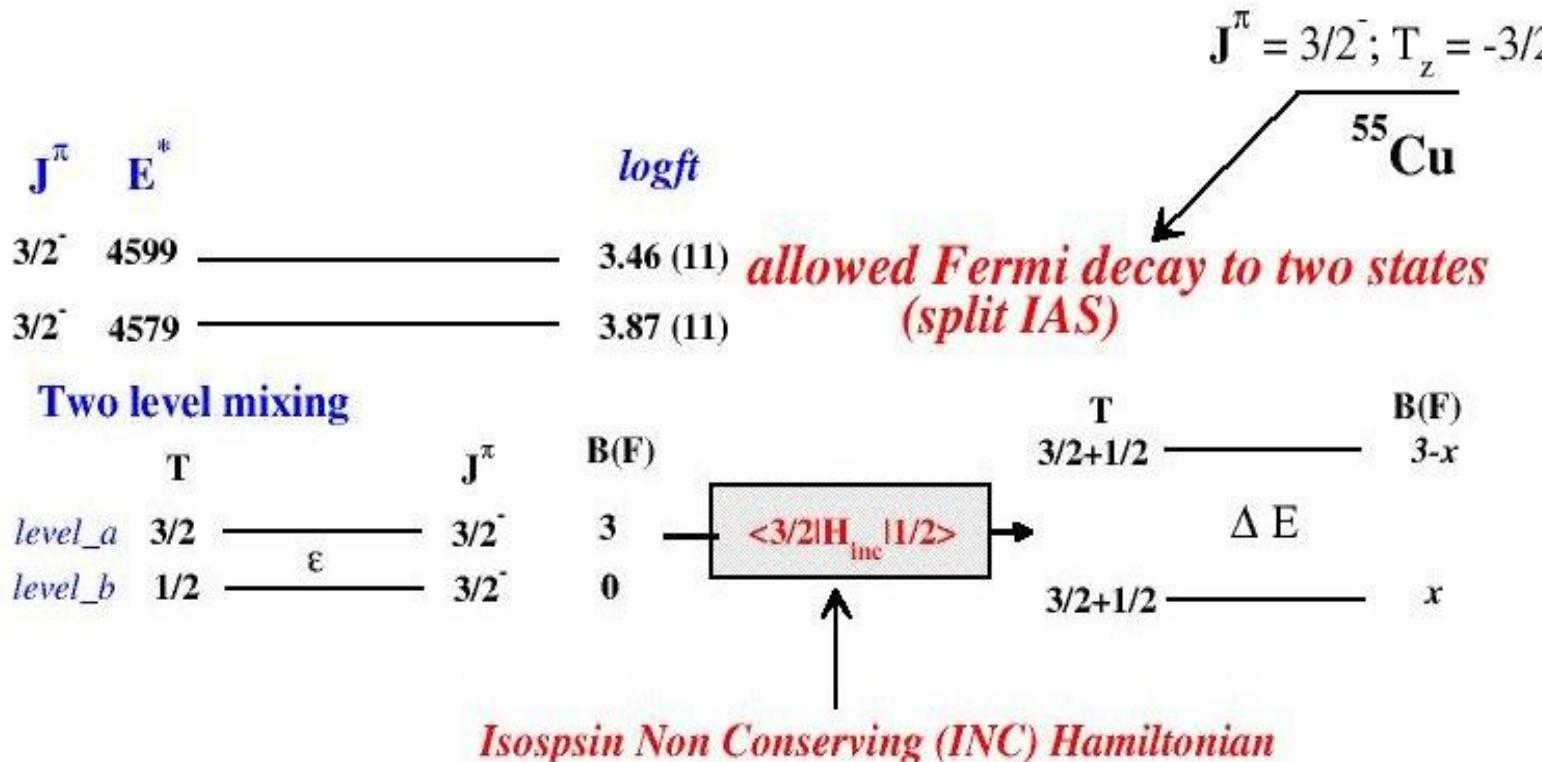
Courtesy V. Tripathi



National Science Foundation  
Michigan State University

EBSS 2014

# Isospin mixing



Courtesy V. Tripathi

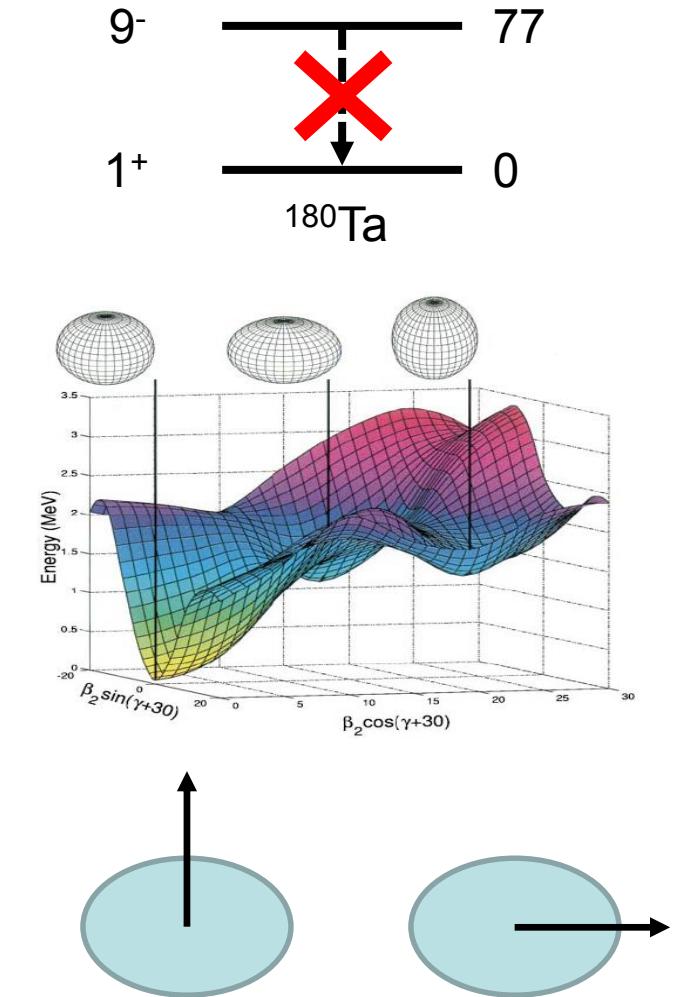


National Science Foundation  
Michigan State University

EBSS 2014

# Isomers

- Excited metastable nuclear states.
- Half-life greater than ns.
- Wide range of excitation energies and half-lives.
- Simple configurations.
  - Many can be related to a few single-particle shell model states.
- Energies and half-lives can inform nuclear models.
- Isomer decay is varied
  - Gamma-ray, Beta-decay, Proton, Fission, ...

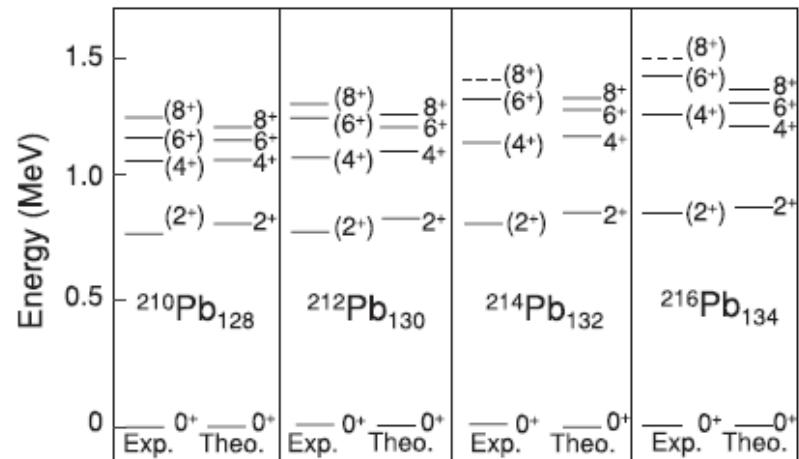
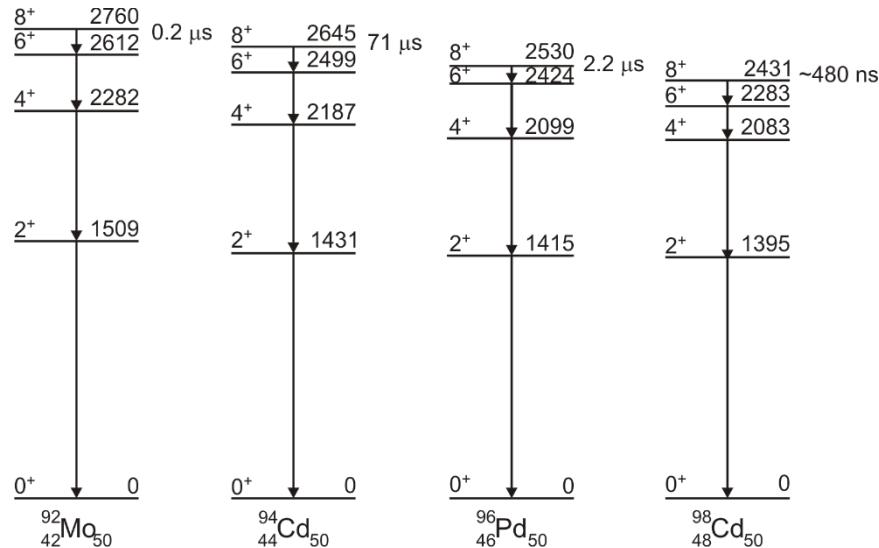


# Question

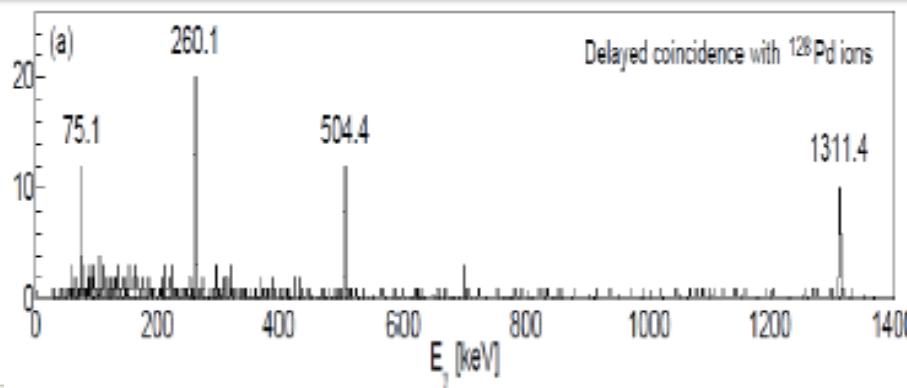
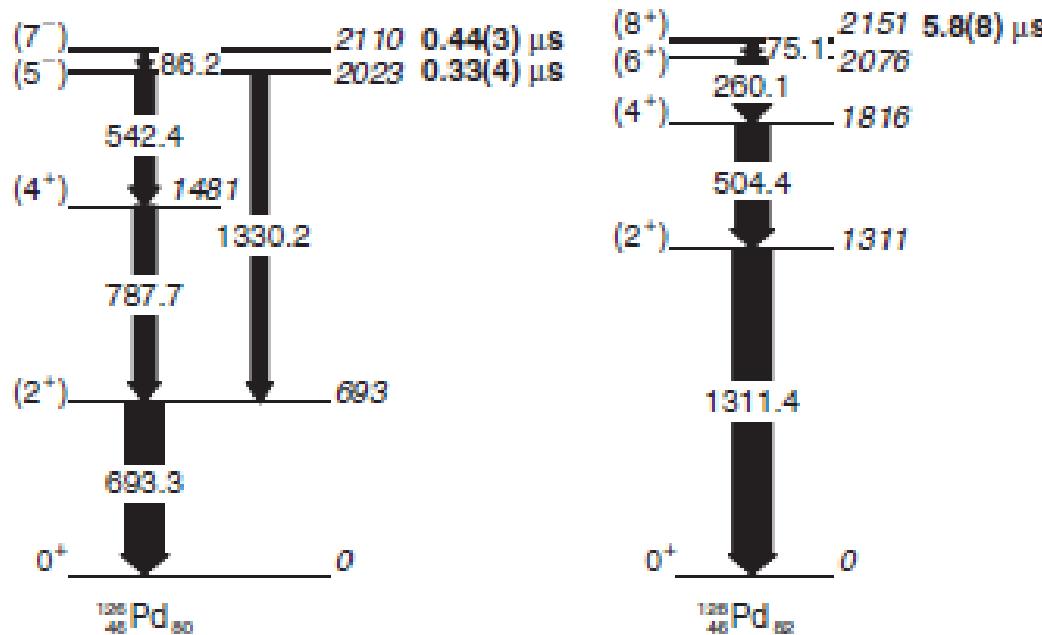
- Consider a pair of nucleons isolated to a  $g_{9/2}$  single-particle state.
- What are the allowed spins?
- A –  $0^+, 1^+, 2^+, 3^+, 4^+, 5^+, 6^+, 7^+, 8^+, 9^+$
- B –  $0^+, 2^+, 4^+, 6^+, 8^+$
- C –  $0^+, 1^+, 3^+, 7^+, 9^+$
- D –  $1^+, 3^+, 7^+, 9^+$
- E –  $0^+, 8^+$

# Isomers

- Pair of particles in well isolated single particle orbital.
  - Protons at  $N = 50$
  - Neutrons at  $Z = 82$
- Low-energy transition.



# $N = 82$



Courtesy S. Nishimura



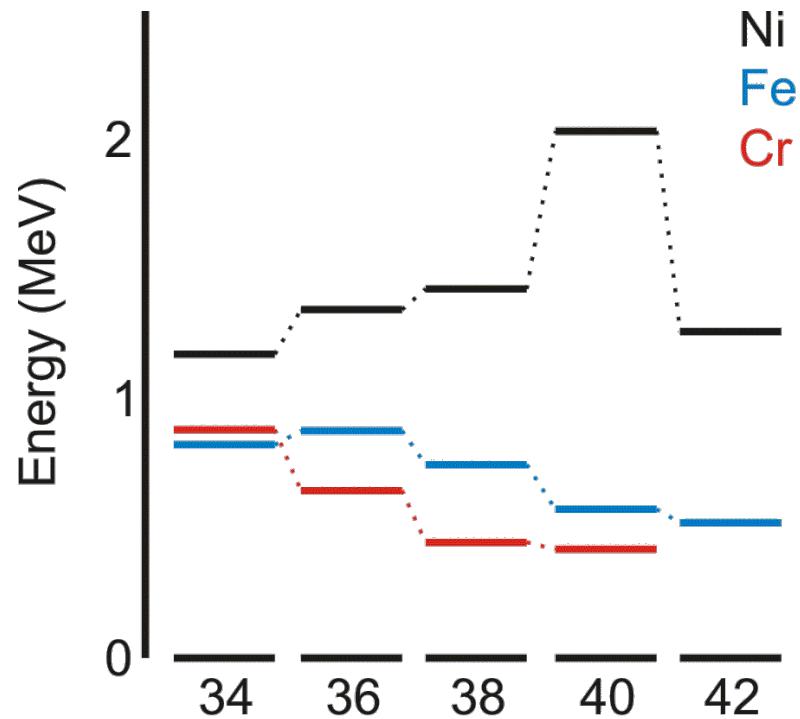
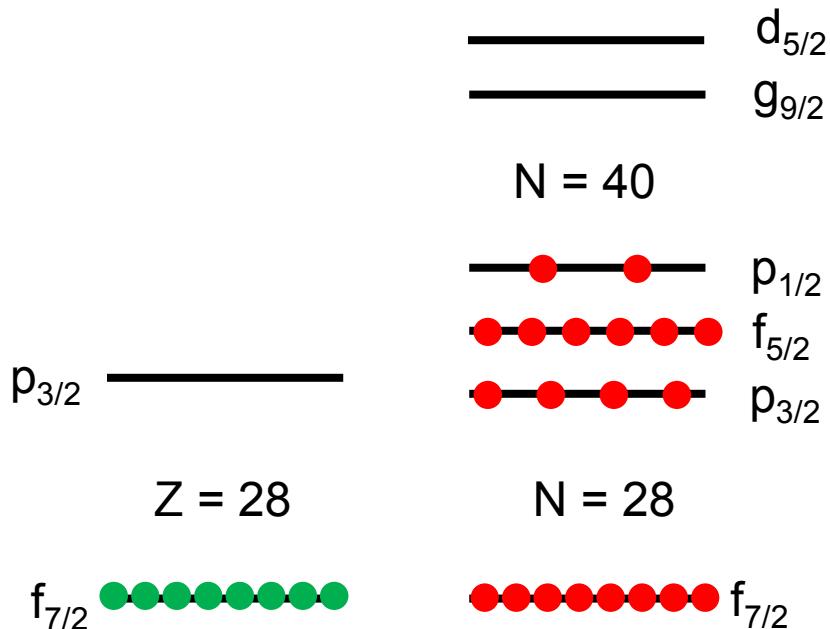
National Science Foundation  
Michigan State University

H. Watanabe et al., Phys. Rev. Lett. 111, 152501 (2013)

EBSS 2014

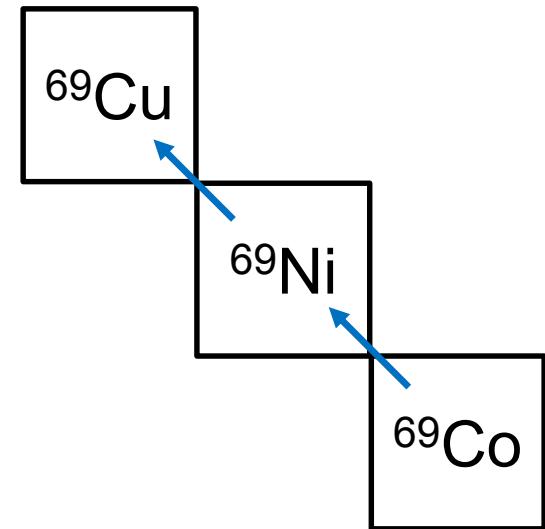
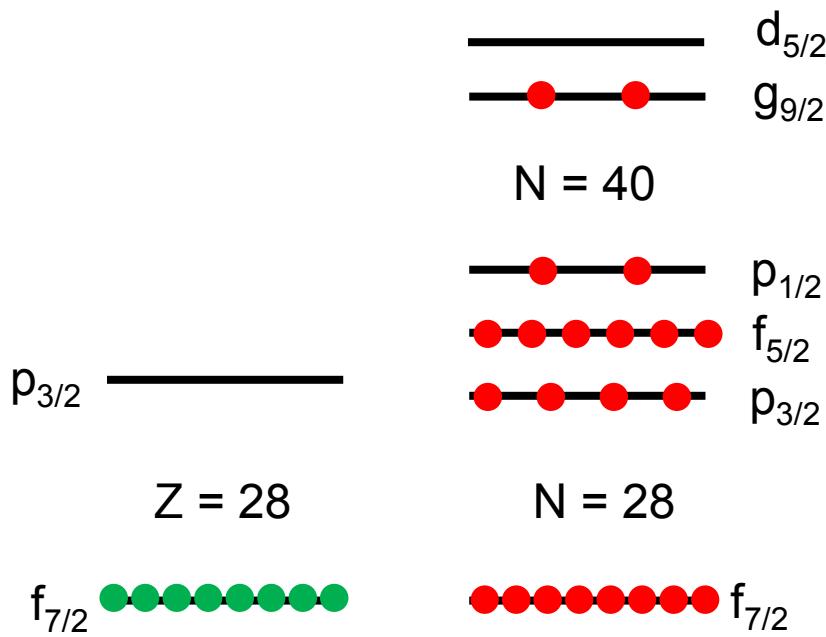
# $N = 40$

- Region around  $N = 40$
- Drop in  $2^+$  energy below  $^{68}\text{Ni}$ .



# $N = 40$

- Region around  $N = 40$
- Drop in  $2^+$  energy below  $^{68}\text{Ni}$ .

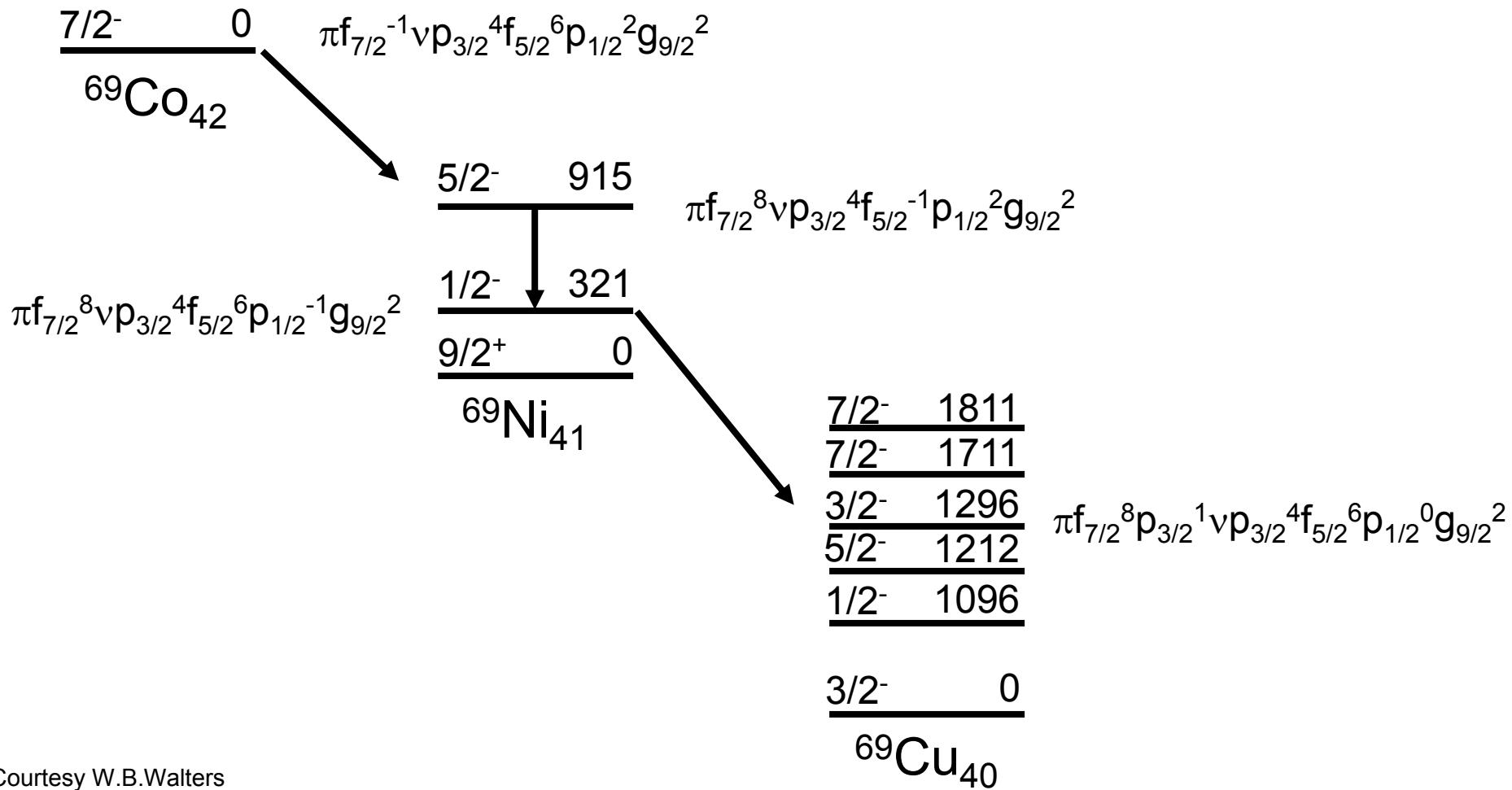


$$M_{fi} = \langle \varphi_f^* | \sigma\tau | \varphi_i \rangle$$

Strong preference for  
spin-flip transition:

$$f_{5/2} \rightarrow f_{7/2}$$

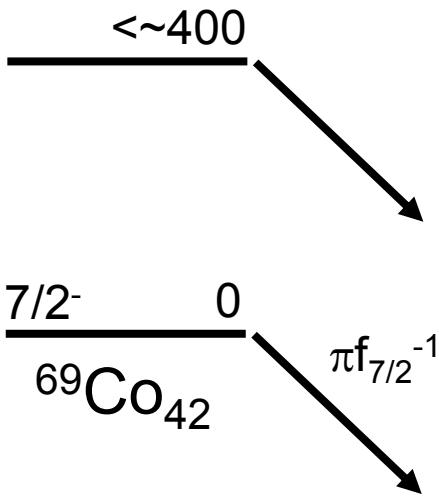
# Mass 69 chain



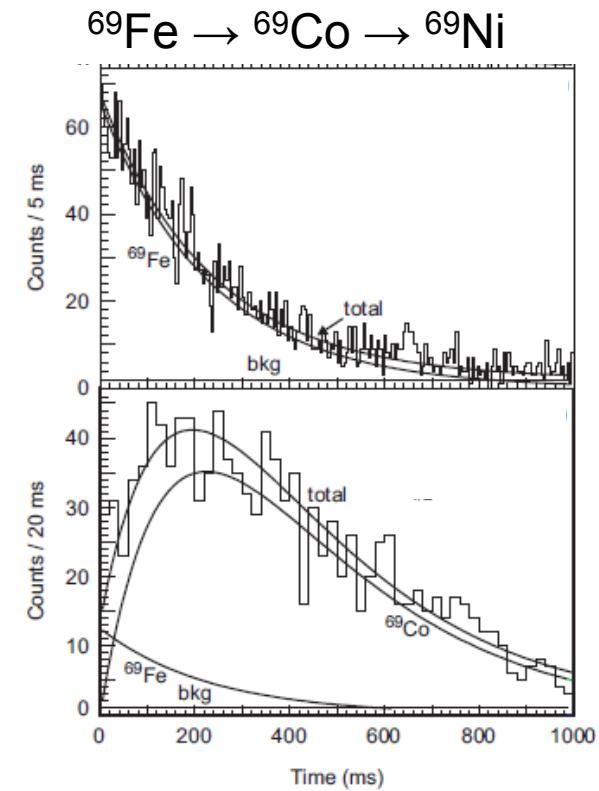
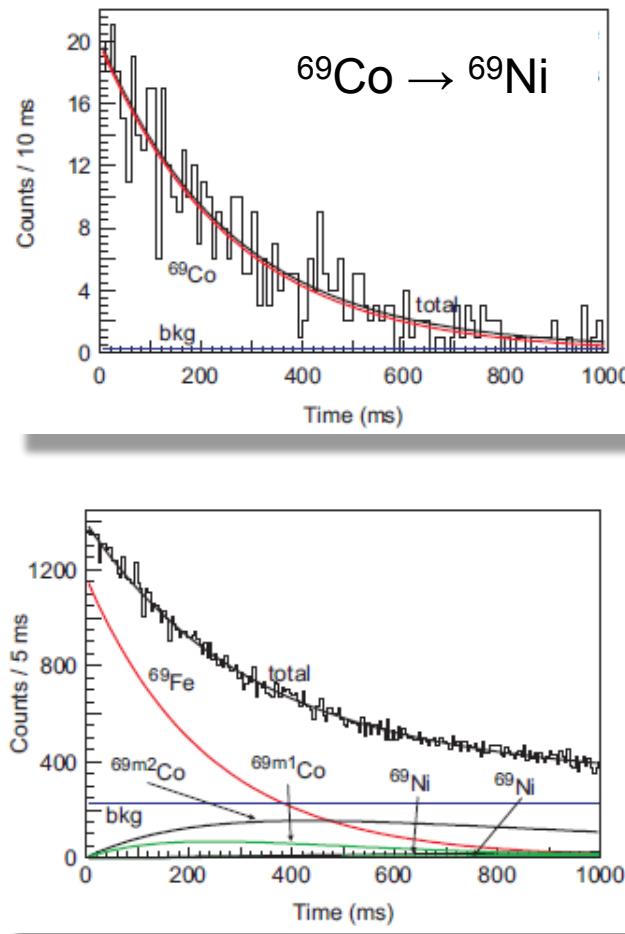
Courtesy W.B.Walters

# $^{69}\text{Co}$ isomer

- Multiple beta-decaying states inferred.



- Population of isomer changes based on production.



# $^{69}\text{Co}$ isomer

- States attributed to excitations across  $Z = 28$  observed throughout the Co, Ni, Cu isotopic chains.
- Require the application if multiple complimentary probes.

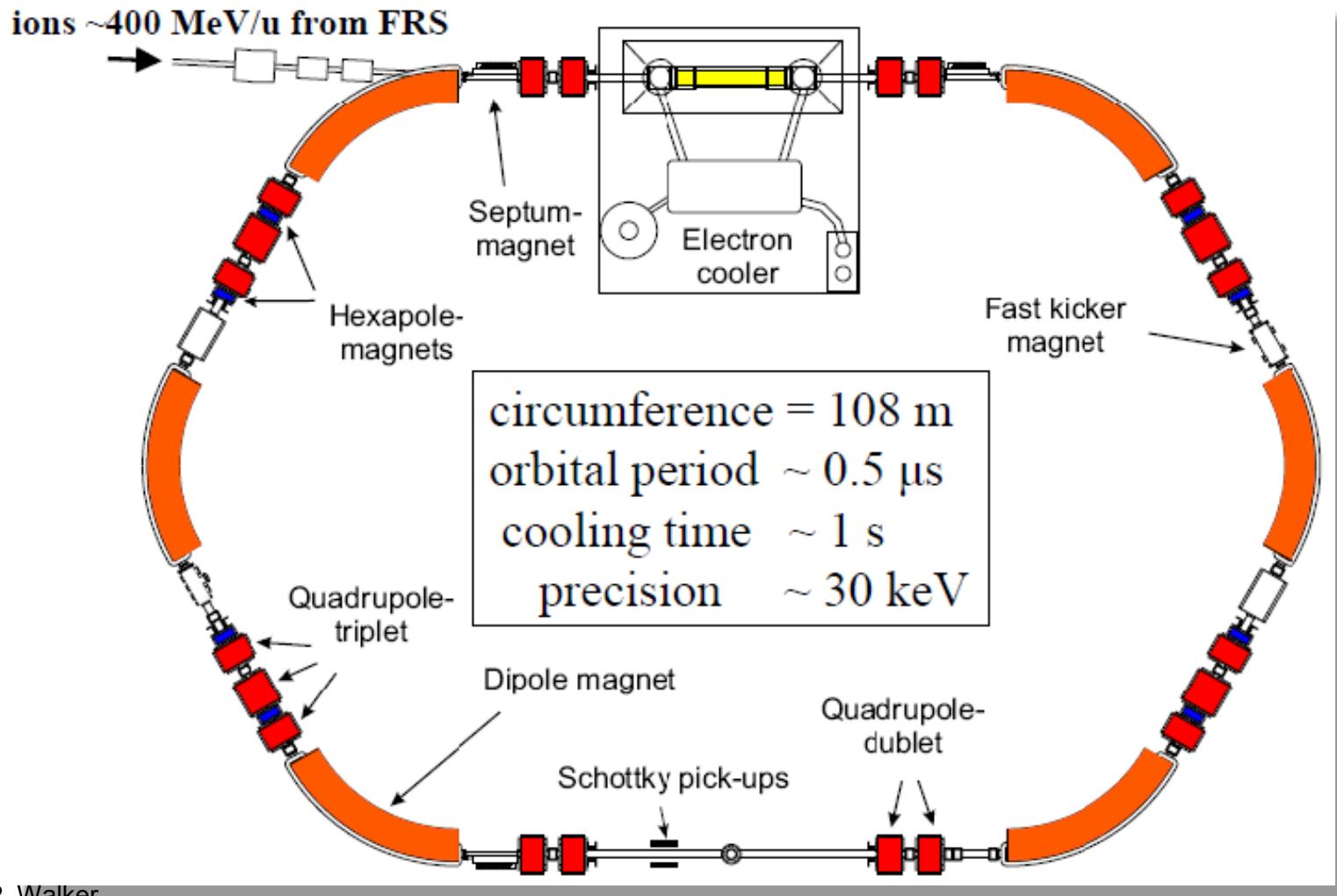
$\pi p_{3/2}^{+1}$   $1/2^- \quad 1095$

$\pi f_{7/2}^{-1}$      $7/2^- \quad 0$      $7/2^- \quad 0$      $7/2^- \quad 0$   
                     $^{65}\text{Co}_{38}$      $^{67}\text{Co}_{40}$      $^{69}\text{Co}_{42}$

# Long-lived Isomers: $^{212}\text{Bi}$

- One proton, three neutrons removed from  $^{208}\text{Pb}$ .  
 $>17^-$  — ?  $> 1900$
- Proton –  $h_{9/2}$
- Neutron –  $i_{11/2}, g_{9/2}$
- Should be amenable to shell model treatment.
- Isomer predicted at 1486 keV.
- Inferred from beta decay at higher energy.  
 $8,9^-$  — 250(30)  
 $1^-$  — 0

# $^{212}\text{Bi}$ : Storage rings



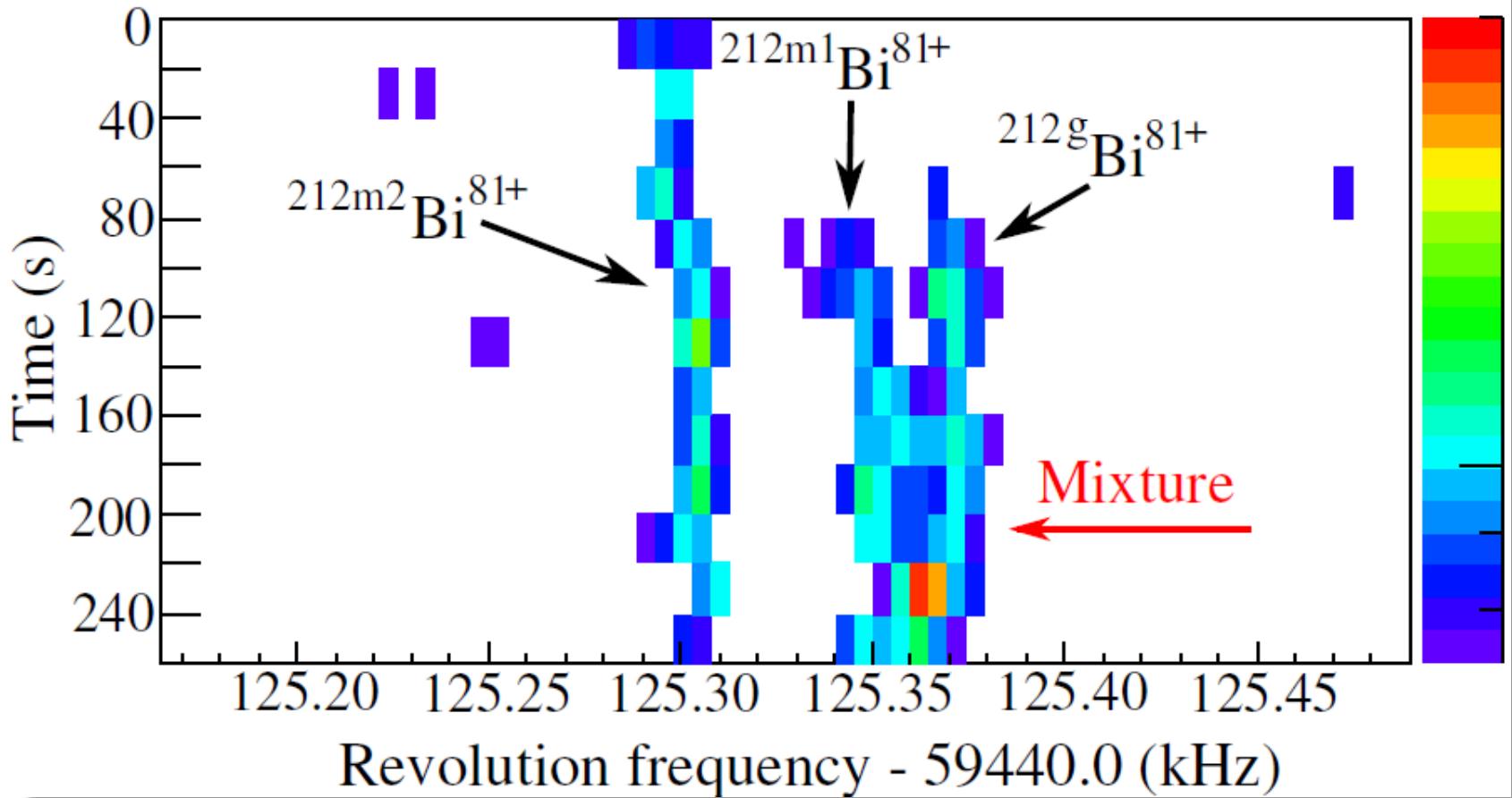
Courtesy P. Walker



National Science Foundation  
Michigan State University

EBSS 2014

# $^{212}\text{Bi}$ : Schottky mass spectrometry



Courtesy P. Walker

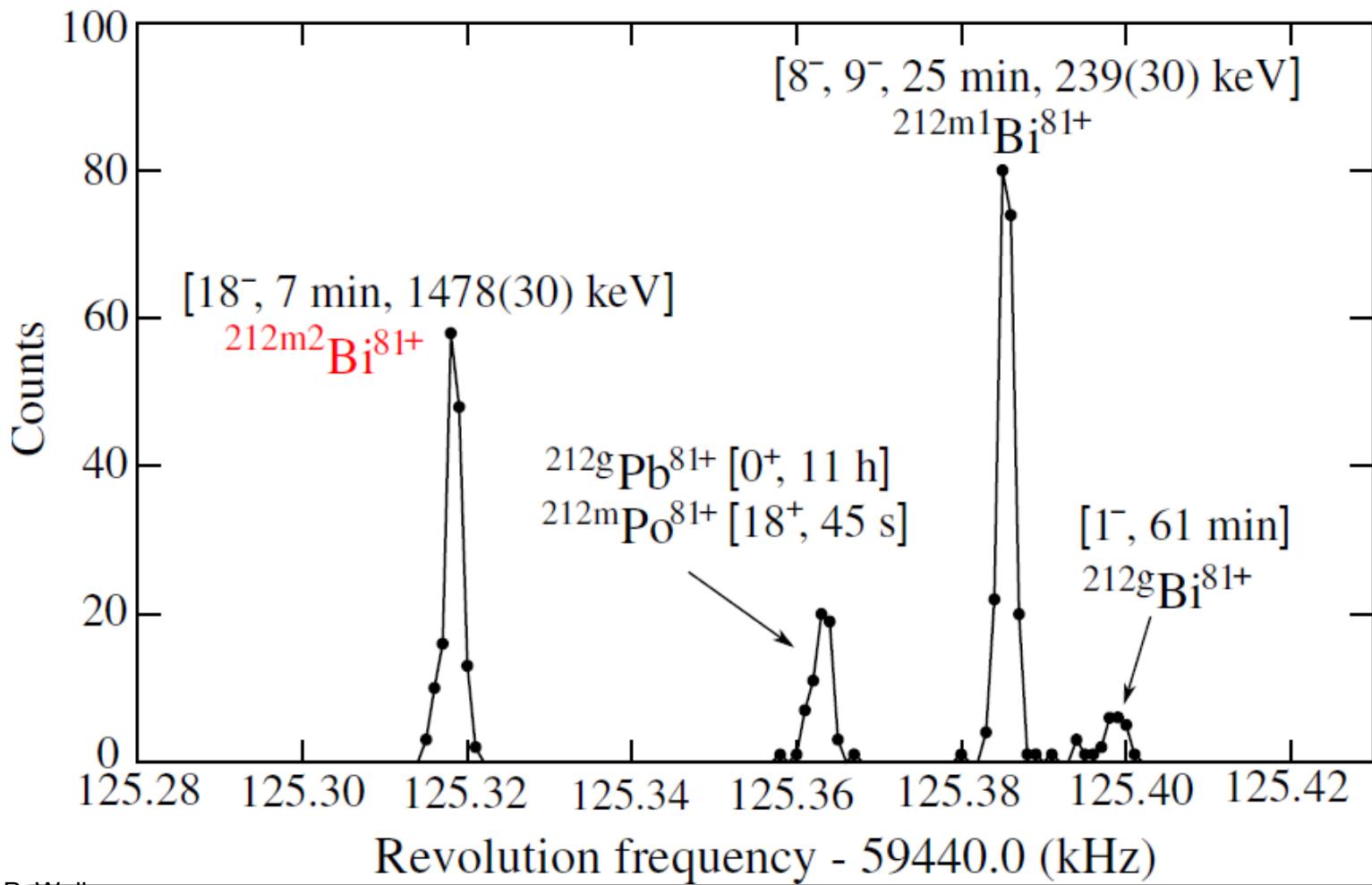


National Science Foundation  
Michigan State University

Chen *et al.*, Phys. Rev. Lett. 110 (2013) 122502

EBSS 2014

# $^{212}\text{Bi}$ : Schottky mass spectrometry



Courtesy P. Walker

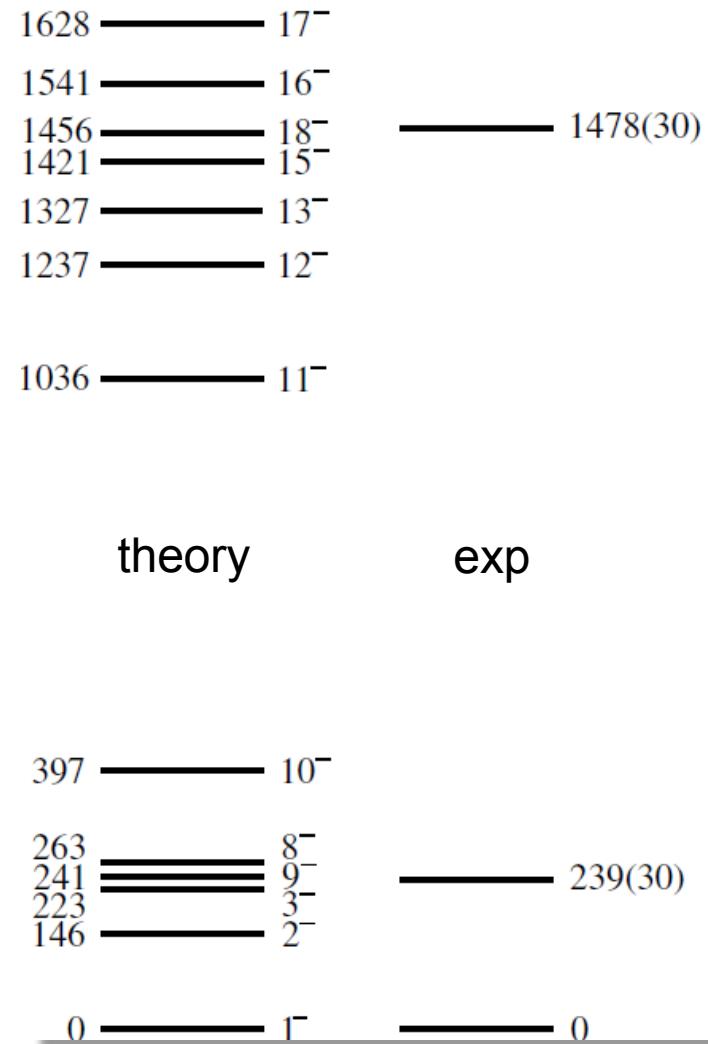


National Science Foundation  
Michigan State University

EBSS 2014

# $^{212}\text{Bi}$

- Half-life of  $^{212}\text{Bi}$ .
  - Previous value 7.0 (3) min
  - Current value > 30 min
  - Difference due to high charge state
- Implies highly converted electron conversion transition.
- New half-life resolves log  $ft$  problem with previous measurement.



Courtesy P. Walker

# Questions



National Science Foundation  
Michigan State University

EBSS 2014